

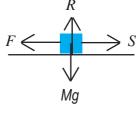
Mechanics 2.8.

Friction

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Consider a particle of mass M, which is on a rough horizontal plane. Given a horizontal force of magnitude S is applied (as in Figure 1), then assuming the particle remains in equilibrium, the magnitude of the frictional force, F, opposing any motion, will be equal to S, i.e. F = S.

If S is gradually increased, then F also increases, as long as the particle remains at rest, so that the equation F = S still holds true. **But**, F cannot increase indefinitely, it can only increase up to a limit F_{MAX} .





How large the frictional force, F, can become is determined by

1. The force between the surfaces in contact and

2. The types of surfaces

The normal reaction, is the vertical force perpendicular to the contact surface. It can be shown that F_{MAX} is proportional to the magnitude of the normal reaction, R. Consequently, $F_{MAX} = \mu \times R$

where μ , known as the Coefficient of (Static) Friction, is a constant, which depends on the roughness of the surface. Slipping will occur if *S* is increased further. **Note:**

Note:

- 1. The frictional force is said to be limiting when it equals its maximum, F_{MAX}
- **2.** The inequality $F \leq \mu R$ is always true
- **3.** A smooth plane gives $\mu = 0$, which means $F_{MAX} = 0$

4. When there is motion, friction is slightly smaller than limiting friction, but unless otherwise informed the assumption that friction = F_{MAX} will be adopted.

Worked Example 1.

A horizontal force of 20 N acts on a particle of mass 7 kg on a rough horizontal plane. Given the particle is on the point of slipping, what is the coefficient of friction, between the particle and the plane?

Solution

Resolving Vertically:

R = mg = 68.67 N

Resolving Horizontally:

$$20 - F = 0, \Rightarrow F = 20 \text{ N}$$

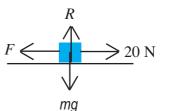


Figure 2



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As the particle is on the point of slipping, fiction is limiting, $F = F_{MAX}$, so:

$$F_{MAX} = \mu R$$

20 = 68.67 μ
 $\Rightarrow \mu = \frac{20}{68.67} = 0.29$ (2 s.f.)

Worked Example 2.

The coefficient of friction between a particle, of mass 8 kg, and a rough horizontal plane is 0.4. Given a horizontal force of 29 N acts on the particle (as in Figure 3) does slipping occur?

Solution

Resolving Vertically:

R = mq = 78.48 N

 $F_{MAX} = 0.4 \times 78.48 = 31 \text{ N} (2 \text{ s.f.})$ Also:

And for equilibrium:

 $F = 29 < 31 = F_{MAX}$, so no motion will occur.

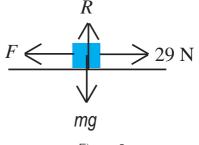


Figure 3

Exercises

- 1. A horizontal force of 15 N acts on a particle of mass 14 kg on a rough horizontal plane. Given the particle is on the point of sliding, what is the coefficient of friction between the particle and the plane?
- 2. A horizontal force of $\frac{3}{2}g$ N acts on a particle of mass 9 kg on a rough horizontal plane. Given the particle is on the point of sliding, what is the coefficient of friction between the particle and the plane?
- 3. The coefficient of friction between a particle, of mass 9.5 kg, and a rough horizontal plane is 0.12. Given that a horizontal force of 12 N acts on the particle, does slipping occur?
- 4. The coefficient of friction between a particle, of mass 6 kg, and a rough horizontal plane is $\frac{1}{3}$. Given that a horizontal force of 2g N acts on the particle, does slipping occur?
- 5. A horizontal force of T N acts on a particle of mass 12 kg, which is on a rough horizontal plane. Given that the particle is on the point of slipping and the coefficient of friction is 0.35, what is T?
- 6. The coefficient of friction between a particle, of mass M kg, and a rough horizontal plane is μ . A horizontal force of $\frac{1}{5}R$ N, where R is the normal contact force, acts on the particle. Given the particle is on the point of slipping what is the value of μ ?

Answers (all to 2 s.f.)

- 1. 0.11 2. $\frac{3}{18} = \frac{1}{6} \approx 0.17$ 3. Yes; slipping occurs; horizontal force = 12 > 11 (F_{MAX}) 4. No; slipping does not occur; horizontal force = $2g \leq 2g$ (F_{MAX}) 5. 41 N 6. 0.20

